

# Simple Design of a Tunable Quadruple-Broadband Terahertz Metamaterial Absorber Based on VO<sub>2</sub>

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**Abstract:** Tunable multi-broadband terahertz (THz) metamaterial absorbers (MAs) can effectively act as THz amplitude modulators, which are the essential components for the future THz communication systems. Till now, various tunable multi-broadband THz MAs including tunable dual-broadband and triple-broadband absorbers have been investigated. However, there are few researches on tunable quadruple-broadband THz MAs. In this work, a simple design of tunable quadruple-broadband THz MA based on VO<sub>2</sub> is proposed. The proposed absorber possesses four broad absorption bands with absorptivity over 90% in frequency ranges of 0.54-2.30 THz, 3.67-5.33 THz, 6.72-8.4 THz and 9.72-11.47 THz, and the corresponding absorption bandwidths reach 1.76 THz, 1.66 THz, 1.68 THz and 1.75 THz, respectively. Moreover, we can dynamically control the absorptivity of four absorption bands by varying VO<sub>2</sub> conductivity. Thus, the proposed absorber possesses the modulation depths of 79.15%, 49.71%, 33.03% and 21.98% at 1.48 THz, 4.46 THz, 7.45 THz and 10.44 THz, respectively. The physical origin of quadruple-broadband perfect absorption is revealed with aid of electric field distributions at resonant frequencies. We also investigate the effects of incidence angle and polarization angle on the quadruple-broadband perfect absorption. The proposed absorber has broad application prospects in THz imaging, modulating, detecting and sensing owing to its excellent absorption characteristics.

**Keywords:** Terahertz, Metamaterial, Quadruple, Tunable, Vanadium Dioxide, Bandwidth

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## 1. Introduction

Today, THz technology has been widely introduced in 5G, 6G communication [1], security [2], biomedicine [3] and nondestructive detection [4]. Particularly, THz MAs have drawn more and more attention because of their critical roles in many THz functional devices. In 2008, Tao and his colleagues [5] firstly proposed the narrowband THz MA. Thereafter, a great number of THz MAs have been developed to obtain multi-band and broadband perfect absorptions [6-16]. However, these MAs are designed and fabricated mainly by using the metal-dielectric-metal structure. Such a configuration unavoidably results in the difficulty in controlling the absorption performances. In fact, the preferred MAs for practical application fields are tunable THz MAs.

Over the past years, tunable THz MAs based on active

materials [17-27] have achieved tremendous progress. Particularly, many researchers have investigated VO<sub>2</sub>-based tunable broadband THz MAs [28-35]. Meanwhile, recently, many efforts have been focused on the design of tunable multi-broadband THz MAs. In future, THz communication systems will require the tunable multi-broadband THz MAs to promote multi-task systems [36]. Moreover, these absorbers are also very useful for sensing applications [37]. In 2020, a tunable dual-broadband THz MA using VO<sub>2</sub> material was designed and investigated by Jiao et al. [38]. This absorber has two broad absorption bands with absorptivity over 90% in frequency ranges of 1.87 THz-4.19 THz and 8.70 THz-10.73 THz, and its absorptivity can be dynamically changed between 2% and 94%. Huang et al. [39] designed an active controllable dual-broadband THz MA with VO<sub>2</sub> resonator, the absorption bandwidths of 80% absorptivity are 0.88 THz and 0.77 THz. Moreover, its

absorptivity can be adjusted from 20% to 90%. In 2022, Feng *et al.* [40] designed a tunable dual-broadband THz MA based on VO<sub>2</sub> material. The absorption bandwidths of 90% absorptivity are 3.4 THz and 3.06 THz, and its absorptivity can be changed from 2% to 100%. In 2023, Ri *et al.* [41] designed a tunable dual-broadband THz MA with slotted VO<sub>2</sub> resonator, the absorption bandwidths of 90% absorptivity can reach 3.41 THz and 3.25 THz. In addition, its absorptivity can be changed from 20% to over 90%. In the latest work [42], a novel tunable triple-broadband THz MA with single VO<sub>2</sub> ring was proposed, the absorption bandwidths of 90% absorptivity were 2.35 THz, 2.30 THz and 2.40 THz, and the absorptivity can be dynamically changed from 20% to over 90%. However, recent researches on tunable multi-broadband MAs are mainly limited to the tunable dual-broadband and triple-broadband THz MAs, no further research on tunable quadruple-broadband THz MA

has been carried out.

In this work, we propose a novel tunable quadruple-broadband THz MA with single VO<sub>2</sub> resonator, whose absorptivity exceeds 90% in the four frequency ranges of 0.54-2.30 THz, 3.67-5.33 THz, 6.72-8.4 THz and 9.72-11.47 THz, and the corresponding absorption bandwidths are 1.76 THz, 1.66 THz, 1.68 THz and 1.75 THz, respectively. Compared with previous tunable multi-broadband THz absorbers, our designed absorber has the excellent characteristics of quadruple-band, broadband, and simple resonant structure. Moreover, the absorptivity of four absorption bands can be continuously adjusted under thermal control. The physical origin of quadruple-broadband absorption is clarified by studying the electric field distributions at resonant frequencies. Finally, we investigate the effects of incidence and polarization angles on quadruple-broadband perfect absorption.

## 2. Design and Simulation

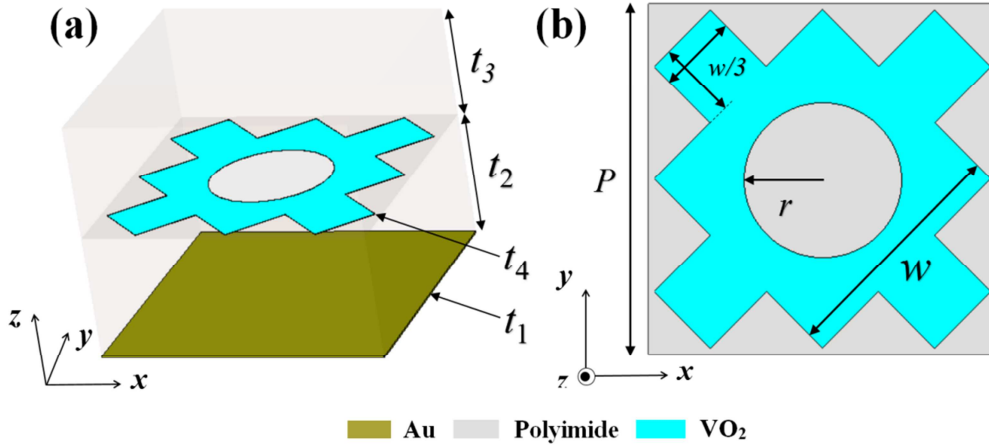


Figure 1. Schematic diagram of the proposed absorber: (a) 3D structure of the unit cell, (b) front view of the unit cell.

The unit cell of proposed absorber possesses the gold-polyimide-VO<sub>2</sub>-polyimide configuration as shown in Figure 1. Such a configuration has already been validated as the efficient absorber structure in the previous studies [41, 42]. The gold ground plane has the thickness of  $t_1 = 0.4 \mu\text{m}$  and the conductivity of  $\sigma = 4.561 \times 10^7 \text{ S/m}$ . The polyimide material has the dielectric constant of  $\epsilon = 3(1 + i0.06)$  [43]. The thickness of VO<sub>2</sub> resonator is  $t_4 = 0.1 \mu\text{m}$  and its optical dielectric constant is represented by the Drude model [44]:

$$\epsilon(\omega) = \epsilon_\infty - \frac{\omega_p^2(\sigma)}{(\omega^2 + i\gamma\omega)} \quad (1)$$

where,  $\epsilon_\infty = 12$  and  $\gamma = 5.75 \times 10^{13} \text{ rad/s}$  stand for the high-frequency permittivity and the collision frequency, respectively. The plasma frequency is given as:

$$\omega_p^2(\sigma) = \frac{\sigma_{\text{VO}_2}}{\sigma_0} \omega_p^2(\sigma_0) \quad (2)$$

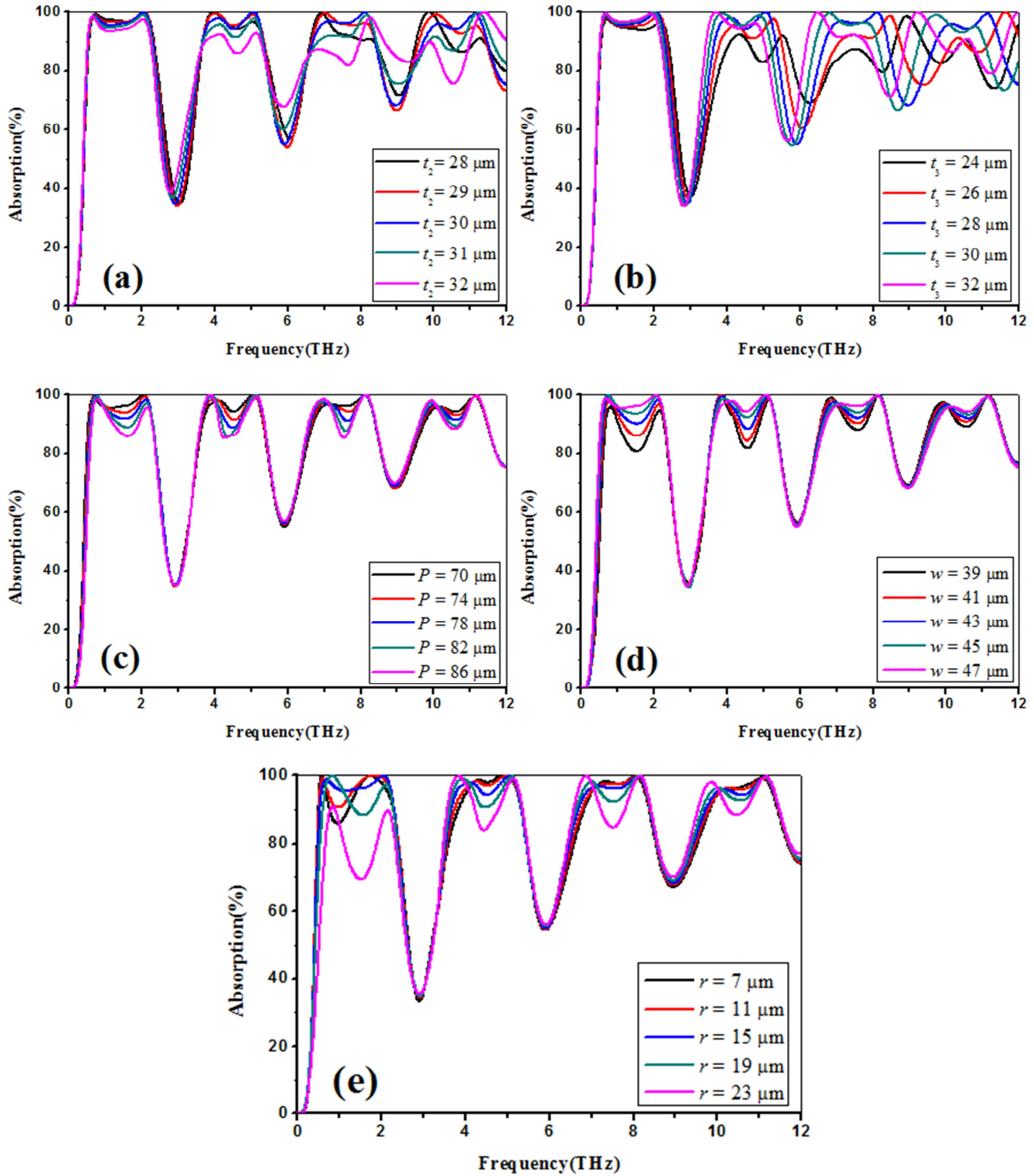
with  $\sigma_0 = 3 \times 10^5 \text{ S/m}$  and  $\omega_p(\sigma_0) = 1.4 \times 10^{15} \text{ rad/s}$ . The conductivities of VO<sub>2</sub> ( $\sigma_{\text{VO}_2}$ ) are  $2 \times 10^5 \text{ S/m}$  and  $200 \text{ S/m}$  at  $T = 350 \text{ K}$  and  $T = 300 \text{ K}$ , respectively [45].

We extracted the geometrical parameters of the unit cell through the optimization process with the frequency-domain solver in a CST Microwave Studio software. In our simulations, unit cell boundary conditions are applied in x- and y- directions and open boundary condition is applied in z-direction. Moreover, the proposed absorber is exposed to normally incident transverse electric (TE) and transverse magnetic (TM) waves. The absorptivity of the proposed absorber can be expressed as  $A(\omega) = 1 - |S_{11}(\omega)|^2 - |S_{21}(\omega)|^2$ , where  $|S_{11}(\omega)|^2$  and  $|S_{21}(\omega)|^2$  stand for reflection and transmission, respectively. For the case of proposed absorber, transmission  $|S_{21}(\omega)|^2$  is close to zero on account of the gold ground plane. Then, the absorptivity can be calculated as  $A(\omega) = 1 - |S_{11}(\omega)|^2$ .

The main objective of optimization process is to simultaneously obtain quadruple-band absorption and broadband absorption at  $T = 350 \text{ K}$ . We first simulated the

absorption performance of proposed absorber for different values of  $t_2$  while other geometrical parameters remain unchanged. Figure 2(a) shows that the proposed absorber possesses four wide absorption bands with absorptivity over 90% for  $t_2 = 30 \mu\text{m}$ . After the thickness of polyimide substrate  $t_2$  is selected, other geometrical parameters should be optimized by turns to further improve the

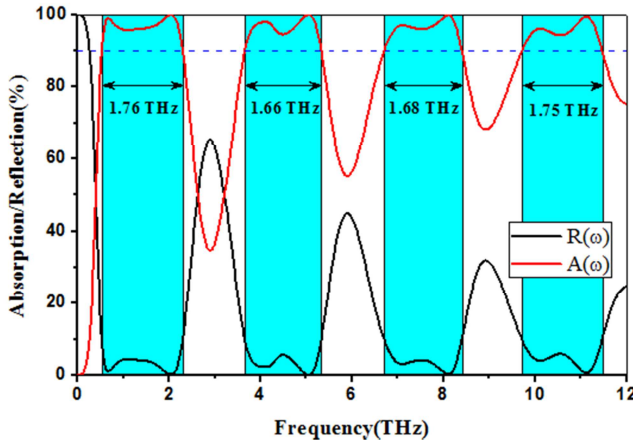
quadruple-broadband absorption. Figure 2(b)-2(e) display the absorption curves of proposed absorber for different values of the thickness of polyimide substrate ( $t_3$ ), periodic length of unit cell ( $P$ ), side length of  $\text{VO}_2$  resonator ( $w$ ), radius of circular hole ( $r$ ), respectively. Consequently, the optimized values of geometrical parameters are  $t_2 = 30 \mu\text{m}$ ,  $t_3 = 28 \mu\text{m}$ ,  $P = 70 \mu\text{m}$ ,  $w = 47 \mu\text{m}$ ,  $r = 15 \mu\text{m}$ .



**Figure 2.** Absorption curves of the proposed absorber with different geometrical parameters: (a)  $t_2$ , (b)  $t_3$ , (c)  $P$ , (d)  $w$  and (e)  $r$ .

### 3. Results and Discussion

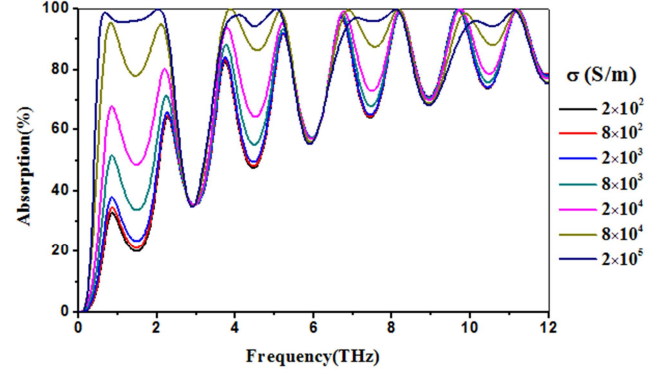
The absorption and reflection curves of the tunable quadruple-broadband THz MA with optimized geometrical parameters are plotted in Figure 3. It can be found that the proposed absorber has eight absorption peaks at 0.68 THz, 2.05 THz, 4.10 THz, 5.06 THz, 7.11 THz, 8.11 THz, 10.14 THz and 11.12 THz with absorptivities of 98.88%, 99.86%, 97.88%, 99.96%, 97.01%, 99.81, 96.01% and 99.39%, respectively. These eight absorption peaks couple together to form four broad absorption bands. The absorptivity of tunable quadruple-broadband THz MA is over 90% in four frequency ranges of 0.54-2.30 THz, 3.67-5.33 THz, 6.72-8.4 THz and 9.72-11.47 THz, and its absorption bandwidths are 1.76 THz, 1.66 THz, 1.68 THz and 1.75 THz, respectively.



**Figure 3.** Absorption and reflection curves of the proposed absorber under TE wave at  $T=350$  K.

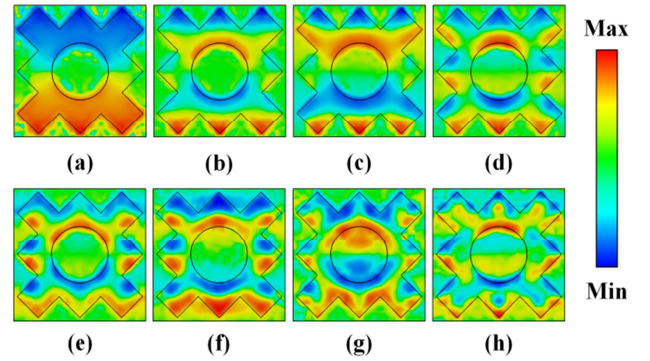
The absorption tunability of proposed absorber is also investigated. The conductivity of VO<sub>2</sub> changes with environmental temperature. Then, since the permittivity of VO<sub>2</sub> is influenced by its conductivity, we are able to tune the absorptivity of proposed absorber under thermal control. As shown in Figure 4, with the increase of conductivity of VO<sub>2</sub>, the absorptivities of four absorption bands continuously increase from 20% to 96.1%, from 47.4% to 94.3%, from 64.2% to 96% and from 73.8% to 94.6%, respectively. The modulation depth, defined as  $MD = (A_m - A_i)/A_m \times 100$  is a critical factor of the tunable MA, where  $A_m$  and  $A_i$  stand for the absorptivities for

metallic and insulator states of VO<sub>2</sub>, respectively [46]. This absorber possesses the modulation depths of 79.15%, 49.71%, 33.03% and 21.98% at 1.48 THz, 4.46 THz, 7.45 THz and 10.44 THz, respectively.



**Figure 4.** Absorption curves of the proposed absorber with different conductivities of VO<sub>2</sub>.

Here, we compared the absorption performances of tunable quadruple-broadband THz MA with other results reported in similar studies (see Table 1). Despite the simple absorber structure as shown in Figure 1, our absorber has good tunable quadruple-broadband absorption performance. It is natural that when the number of absorption bands increases in the limited simulation frequency range of 0-12 THz, the bandwidth of each absorption band becomes narrower. So, our absorber has broad application prospects in THz modulators, sensors, switches and detectors.



**Figure 5.** Electric field ( $E_z$ ) distributions at resonant frequencies: (a)  $f_1=0.68$  THz, (b)  $f_2=2.05$  THz, (c)  $f_3=4.10$  THz, (d)  $f_4=5.06$  THz, (e)  $f_5=7.11$  THz, (f)  $f_6=8.11$  THz, (g)  $f_7=10.14$  THz, (h)  $f_8=11.12$  THz.

**Table 1.** Comparison of the proposed absorber with other studies.

Ref.	Absorption Bandwidth (THz)	Adjustable Material	Tunable Range (%)	Thickness ( $\mu\text{m}$ )
[38]	2.32, 2.03	VO <sub>2</sub>	2-94	12.28
[39]	0.88, 0.77	VO <sub>2</sub>	20-90	35.3
[40]	3.40, 3.06	VO <sub>2</sub>	2-100	25.51
[41]	3.41, 3.25	VO <sub>2</sub>	20-90	27.8
[42]	2.35, 2.30, 2.40	VO <sub>2</sub>	20-90	44.4
This work	1.76, 1.66, 1.68, 1.75	VO <sub>2</sub>	20-96	58.5

To illustrate the physical origin of quadruple-broadband perfect absorption, we studied the electric field ( $E_z$ )

distributions at the eight resonant modes ( $f_1, f_2, f_3, f_4, f_5, f_6, f_7$  and  $f_8$ ). The simulated electric field ( $E_z$ ) distributions on the



x-y plane are plotted in Figure 5. As shown in Figure 5(a), at  $f_1=0.68$  THz, the strong electric field concentrates in lower and upper areas of VO<sub>2</sub> resonator, thus producing a dipole resonance. At  $f_2=2.05$  THz, the electric field is strongly localized in the outer and inner edges except for left and right sides of VO<sub>2</sub> resonator as shown in Figure 5(b). Such a distribution produces a quadrupole resonance. Thus, the first broad absorption band is attributed to the dipole and quadrupole resonances. As shown in Figure 5(c)-5(h), at  $f_3=4.10$  THz,  $f_4=5.06$  THz,  $f_5=7.11$  THz,  $f_6=8.11$  THz,  $f_7=10.14$  THz and  $f_8=11.12$  THz, the electric fields are strongly distributed on the inner and outer edges of VO<sub>2</sub> resonator, thus generating the high-order resonances. So, the second, third, and fourth broad absorption bands originate from the combination of similar high-order resonances.

Moreover, we further investigated the physical origin of quadruple-broadband absorption by means of LC circuit resonance and standing wave resonance. In accordance with refs. [47, 48], the resonant frequency of MA is calculated as:

$$f_j \approx (2j-1) \frac{c}{2nl}, j=1,2,3,\dots \quad (3)$$

where  $c$ ,  $l$ , and  $n$  stand for the light speed in vacuum, the

length of resonator, and the index of dielectric substrate, respectively. According to Eq. (3), the fundamental mode ( $j=1$ ) and its odd resonant modes are only valid. The absorption peaks of MA originate from these resonance modes. For example, the resonant frequency for the case of  $j=2$  must be 3 times greater than the resonant frequency of  $j=1$ . Table 2 shows the resonant frequencies of the proposed absorber with different VO<sub>2</sub> conductivities (see Figure 4). Here,  $f_{\text{average}}$  are the average values of resonant frequencies for the cases of  $f_1$ - $f_8$ , and  $f_{\text{theoretical}}$  are the theoretical frequencies calculated by Eq. (3). It can be seen from Table 2 that the average of second resonant frequencies ( $f_{2,\text{av}}=2.20$  THz) is approximately 3 times of the average of first resonant frequencies ( $f_{1,\text{av}}=0.82$  THz). Similarly,  $f_{3,\text{av}}=3.82$  THz,  $f_{4,\text{av}}=5.19$  THz,  $f_{5,\text{av}}=6.81$  THz,  $f_{6,\text{av}}=8.19$  THz,  $f_{7,\text{av}}=9.79$  THz and  $f_{8,\text{av}}=11.20$  THz are roughly five, seven, nine, eleven, thirteen and fifteen times of  $f_{1,\text{av}}=0.82$  THz, respectively. We can also know that there are some errors between  $f_{\text{average}}$  and  $f_{\text{theoretical}}$ . The reason is that Eq. (3) neglects the dielectric dispersion of polyimide layer. Consequently, we can conclude that the quadruple-broadband perfect absorption is attributed to the fundamental and high-order resonances of VO<sub>2</sub> resonator.

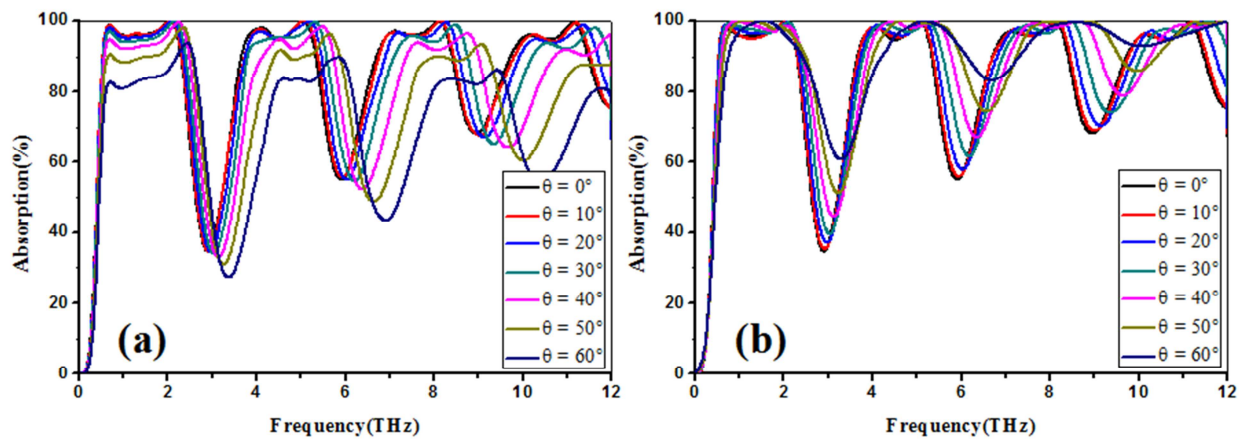


Figure 6. Absorption curves of the proposed absorber for different values of incidence angle at (a) TE and (b) TM waves.

Table 2. Resonant frequencies of the proposed absorber with different values of VO<sub>2</sub> conductivity.

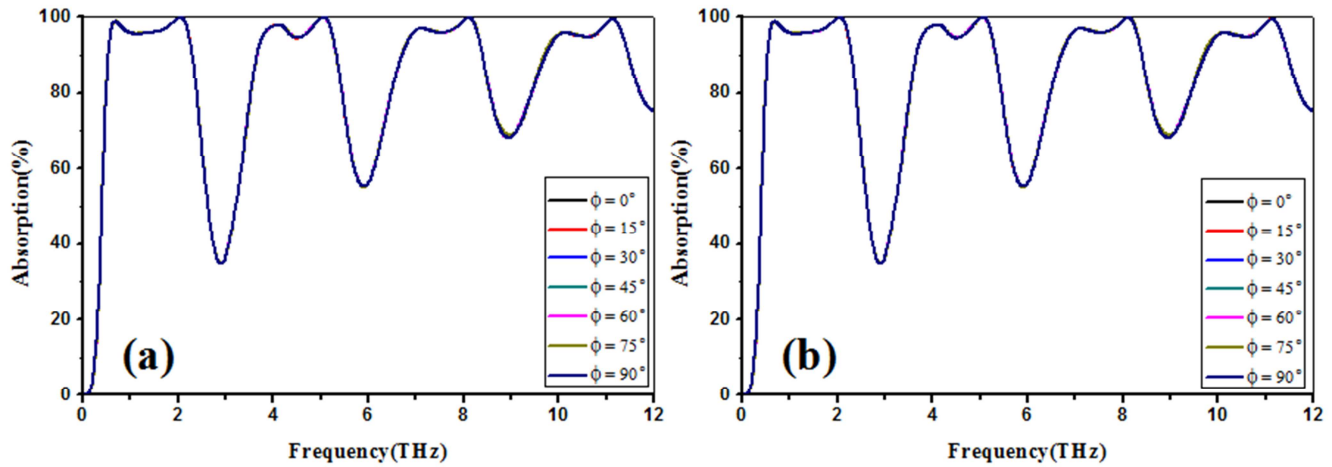
Conductivity of VO <sub>2</sub> (S/m)	Resonant frequency (THz)							
	$f_1$	$f_2$	$f_3$	$f_4$	$f_5$	$f_6$	$f_7$	$f_8$
200	0.86	2.28	3.75	5.24	6.72	8.22	9.70	11.22
800	0.86	2.28	3.75	5.23	6.72	8.22	9.70	11.22
2000	0.86	2.26	3.75	5.23	6.72	8.22	9.70	11.22
8000	0.86	2.24	3.76	5.23	6.74	8.22	9.72	11.20
20000	0.85	2.21	3.79	5.20	6.76	8.20	9.75	11.20
80000	0.82	2.11	3.89	5.14	6.90	8.17	9.87	11.18
200000	0.68	2.05	4.10	5.06	7.11	8.11	10.14	11.12
$f_{\text{average}}$	0.82	2.20	3.82	5.19	6.81	8.19	9.79	11.20
$f_{\text{theoretical}}$	-	2.46	4.10	5.74	7.38	9.02	10.66	12.30

In order to examine the incidence angle dependence of tunable quadruple-broadband THz MA, we analyzed the absorption curves of proposed absorber with different incidence angles under TE and TM waves. As shown in Figure 6(a), the increase of incidence angle under TE wave results in

the blue-shift of four absorption bands, but the absorptivity of each absorption band still remains over 80% for large incidence angle of 50°. Under TM wave, the increase of incidence angle also results in the blue-shift of four absorption bands as shown in Figure 6(b), but the absorptivity of each

absorption band still exceeds 90% for large incidence angles up to 60°. Thus, our absorber possesses good incidence angle

stability.



**Figure 7.** Absorption curves of the proposed absorber for different values of polarization angle at (a) TE and (b) TM waves.

Finally, we simulated the absorption performance of proposed absorber for different values of polarization angle at TE and TM waves. Our designed absorber possesses good polarization-insensitivity owing to the fourfold rotational symmetry as shown in Figure 7.

## 4. Conclusion

Until now, various designs on tunable dual-broadband/triple-broadband THz MAs have been proposed. However, no further research on the tunable quadruple-broadband THz MA has been done. In this work, we have proposed a simple design of tunable quadruple-broadband THz MA based on VO<sub>2</sub>. Simulation results show that the proposed absorber has four broad absorption bands with absorptivity above 90% in frequency ranges of 0.54-2.30 THz, 3.67-5.33 THz, 6.72-8.4 THz and 9.72-11.47 THz, and the corresponding absorption bandwidths reach 1.76 THz, 1.66 THz, 1.68 THz and 1.75 THz, respectively. The absorptivities of four absorption bands can be dynamically tuned from 20% to 96.1%, from 47.4% to 94.3%, from 64.2% to 96% and from 73.8% to 94.6%, respectively. The overlap of fundamental and high-order resonances on the single VO<sub>2</sub> resonator results in the quadruple-broadband perfect absorption. Furthermore, the proposed absorber possesses wide incidence angle stability and polarization-insensitivity. Thus, the proposed absorber has broad application prospects in THz imaging, modulating, detecting and sensing.

## Competing Interests

The authors declare no competing interests.

## Author Contributions

K. J. Ri conceived the idea, performed the simulations and

wrote the manuscript. D. S. Pak analyzed the results and assisted the revision of the manuscript. C. H. Ri supervised the entire project. All authors have read and approved the final manuscript.

## Data Availability

All data used to support the findings in this study are included within the paper.

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